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TWO EXPERIMENTS ON STATISTICAL IMAGE SEGMENTATION

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TWO EXPERIMENTS ON STATISTICAL IMAGE SEGMENTATION

Recently there has been a considerable research interest in applying statistical pattern recognition theory to image segmentation. As the image is rich in statistical information, effective segmentation of images into meaningful parts can be performed by using statistical techniques. In this report, we present segmentation results on infrared and reconnaissance images using two different statistical pattern recognition methods.

The first experiment is on the Alabama data base infrared images using the Fisher's linear discriminant analysis [1]. To preserve the inter-pixel dependence as much as possible, measurements are taken in the form of a 3 x 3 matrix. That is we are dealing with matrix measurements instead of vector measurements as typically considered in statistical pattern recognition. Let x be a matrix measurement and X_i , i = 1,2 be the collection of n_i measurements belonging to the ith class. The two classes considered are the target area and the background area. Define the sample mean matrix and the scatter matrices as

$$M_{i} = \frac{1}{n_{i}} \sum_{x \in X_{i}}^{x}, \qquad i = 1,2$$

$$S_{i} = \sum_{x \in X_{i}}^{x} (x - m_{i}) (x - m_{i})'$$

$$M = \frac{1}{n} \sum_{x \in X_{i}}^{x} = \text{mean of all samples; } n = n_{1} + n_{2}$$

$$S_{w} = S_{1} + S_{2} = \text{pooled scatter matrix}$$

Then the Fisher's linear discriminant computes

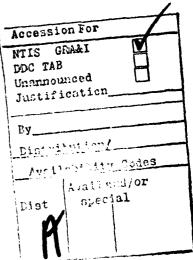
$$y = w'x + \omega_0$$

where W = weight matrix

=
$$\alpha$$
 n S_w⁻¹ (m₁ - m₂); α is an arbitrary constant

$$\omega_{O} = -m'w$$





with w, x and m converted into vector form before computing y which is a scalar quantity. Decision is to choose class 1 if $y \ge 0$ and class 2 otherwise. For each infrared picture a 62 x 62 subimage that contains target(s) is used for the segmentation study. Only one picture is needed for computing the statistical parameters. Table 1 lists the mean and scatter matrices of the first picture considered. These parameters are used in all 18 pictures as tabulated in two sets in Table 2a. Table 2b is a description of the nature of target(s) in each picture along with the aspects. Fig. 2a and Fig. 3a are the original pictures (in two-level display) of Set I and Set II respectively. Figs. 2b and 3b are segmentation results with the bright regions for targets (hot objects). It is seen that the targets are clearly segmented from the background in all pictures. The results are somehwat better than those reported by Ahuja et.al. [2]. The object boundaries can be completely extracted from segmented images by using the cross (Robert) gradient and Sobel operator as shown in Figs. 2c, d and 3c, d.

The second experiment is on the reconnaissance images using two statistical features. Figs. 4 shows all 22 pictures considered. Only a portion of each picture is digitized into a 1024 x 1024 image for computer study. Each image contains one or several objects made of metals. Each image is divided into 256 subimages of size 64 x 64 each. For each subimage, compute a texture feature using co-occurrence statistics as defined in [3] and a gradient feature which is a count of the number of large gradient picture elements as defined in [4]. The coordinates (x,y) of pixels with ten largest feature values are tabulated in order of decreasing value in Table 3 for all images. If we divide the image into 16 x 16 subimages, coordinate x is the subimage column number counted from left to right and coordinate y is the row number counted from top to bottom. A careful

analysis of the tabulated results indicates that over 95% of targets are identified correctly by at least one of the two features. However a number of non-target subimages are also identified. Performance improvement may be available by using additional features and the probabilistic labelling of feature importance. Further results will be reported in the near future.

REFERENCES

- 1. R. O. Duda and P. E. Hart, "Pattern Classification and Scene Analysis," Interscience Publication, pp. 151-154, 1973.
- 2. N. Ahuja, A. Rosenfeld and R. M. Haralick, "Neighbor gray levels as features in pixel classification," Pattern Recognition, vol. 12, no. 4, pp. 251-260, 1980.
- 3. C. H. Chen, "On statistical and structural feature extraction," in "Pattern Recognition and Artificial Intelligence," edited by C. H. Chen, pp. 135-144, Academic Press, 1976.
- 4. C. H. Chen, "On three mathematical problems in image science," in "Image Science Mathematics" Symposium Proceedings, pp. 163-167, 1976.

Table 1 (Figure 1)

*** MEAN MOTRIX OF TARGET ***

- 0. 17251E 03 0. 17714E 03 0. 17885E 03
- 0.17579E 03 0.18043E 03 0.18189E 03
- 0.17320E 03 0.17755E 03 0 1.85/E 03

*** SCATTER MATRIX I ***

- O. 11441E 09 O 82116E 08 O. 56400E 68
- 0.82116E 09 0.88494E 08 0.67940E 08
- 0.56400E 08 0.67940E 08 0.8002LE 08

*** MEAN MATRIX OF BACKOROUND ***

- 0.40578E 02 0.39674E 02 0.38519E 02
- 0.34385E 02 0.33481E 02 0.32475E 02
- 0.81898E 02 0.81102E 02 0.80285E 02

*** SCATTER MATRIX II ***

- 0. 21476E 09 0. 15418E 09 0. 12317E 09
- O. 154185 OP O 16979E OP O 14295E OP
- 0. 12317E 09 0. 14295E 09 0. 1875!E 09

*** SAMPLE SCATTER MATRIX ***

- 0. 32917E 09 0. 23529E 09 0. 17957E 09
- O. 23629E O9 O. 25829E OP O. 21089E O9
- 0.17957E 09 0.21089E 09 0.26753E 09

*** NEIGHT MATRIX ***

- 0. 20839E-02 0. 22701E-01 0. 24455E-02
- C. 100/52E-01 C. 104/5/E-01 C 106/78E-01
- 0.10451E-0.0 10599E-0.0 105004E-0

SET I:

1	2	3
4	5	6
7	8	9

SET II:

10	11	12
13	14	15
16	17	18

Table 2a

File No.	Target(s)	Aspect(s)
1	T	S
2	T	3F
3	T	3F
4	T	S
5	· T	F
6	'T	3 F
7	${f T}$	3 R
8	T,J	3R,3F
9	$\mathtt{T,}J$	S,S
10	Ţ	3F
11	T	S
12	J	3R
13	${f T}$, ${f J}$	3R,3F
14	'T	F
15	T	S
16	Т	3R
17	T	F
18	${f T}$	S

Legend: J = jeep T = tank S = side F = front R = rear3 = 3/4 view

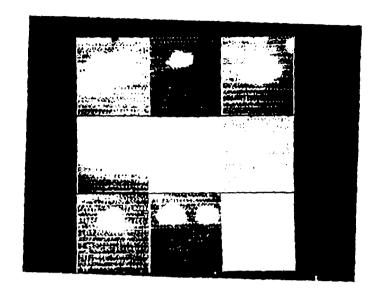


Fig. 2a

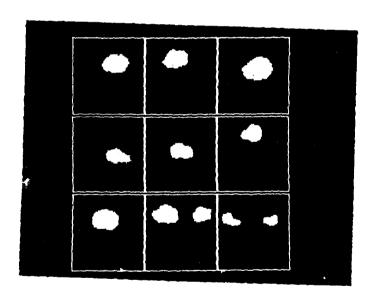


Fig. 2b

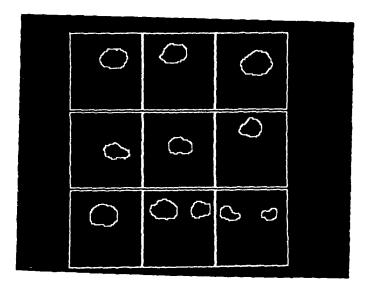
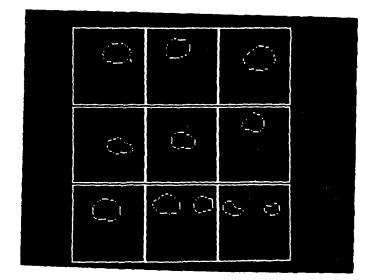


Fig. 2c



(.4)

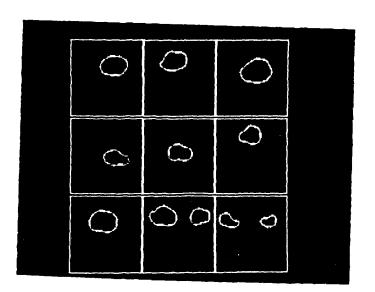


Fig. 28

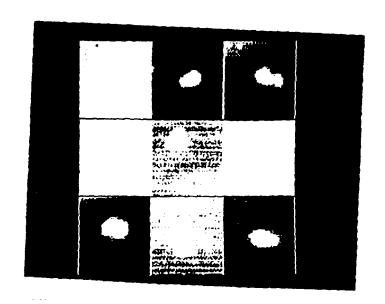


Fig. 3a

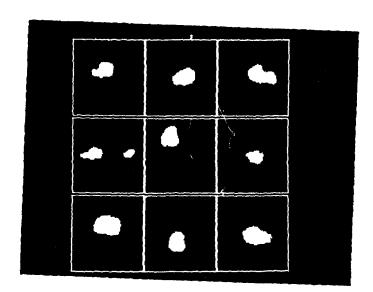


Fig. 3b

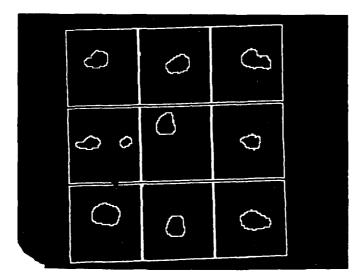
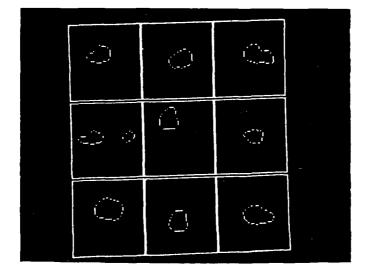


Fig. 3c



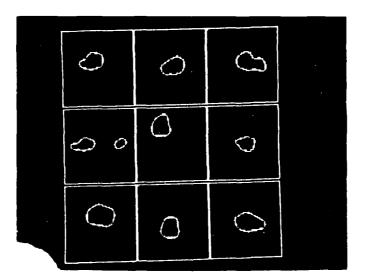




Fig. 4a File 1

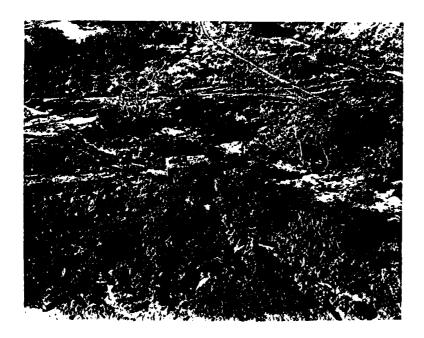


Fig. 4b File 2

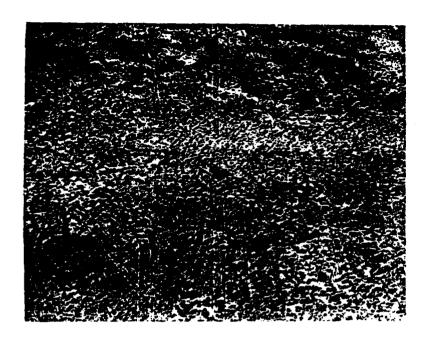


Fig. 4c File 3

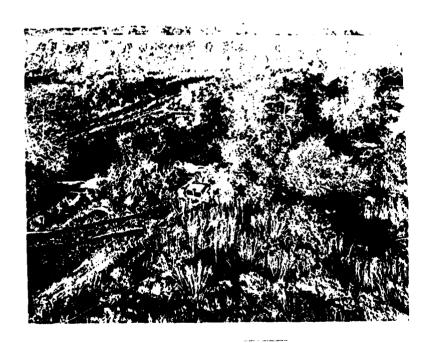


Fig. 4d File 4

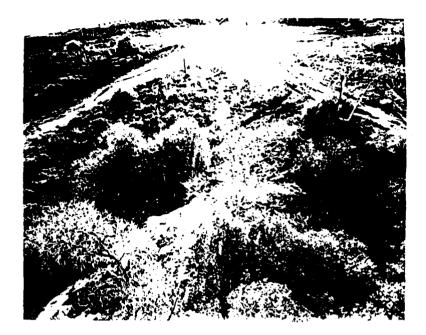


Fig. 4e File 5



Fig. 4f File 6



Fig. 4g File 7

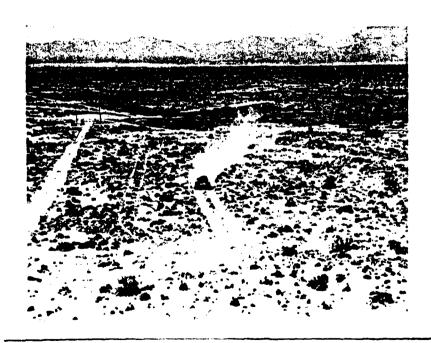


Fig. 4h File 8

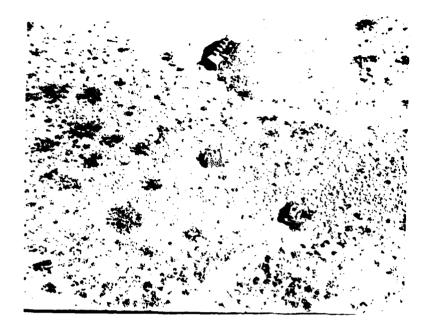


Fig. 4i Fi*le* 9



Fig. 4j File 10



Fig. 4k File 11

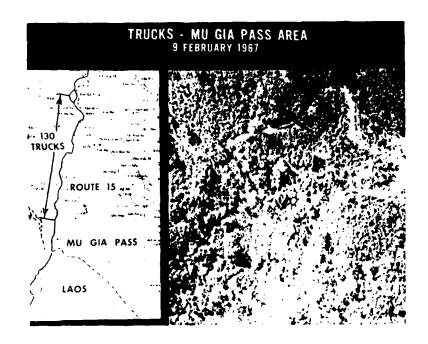


Fig. 40 File 12

Sound to Belleville Just Brown and who



Fig. 4m File 13



Fig. 4n File 14



Fig. 40 File 15

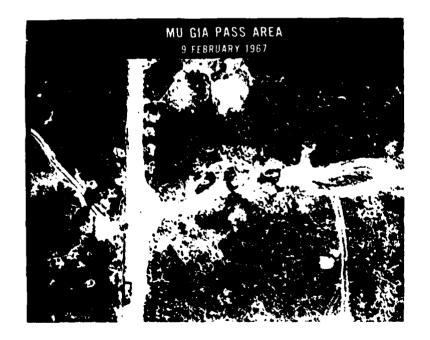


Fig. 4p File 16

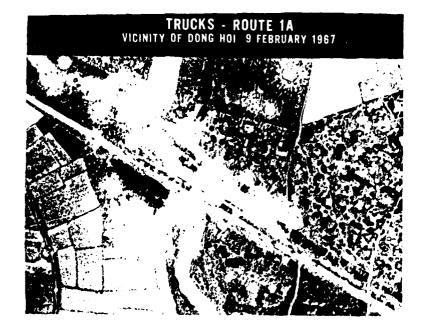


Fig. 4q File 17



Fig. 4r File 18

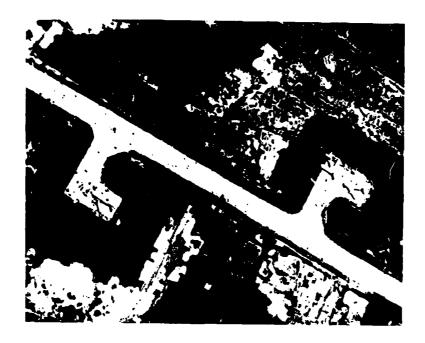


Fig. 4s File 19

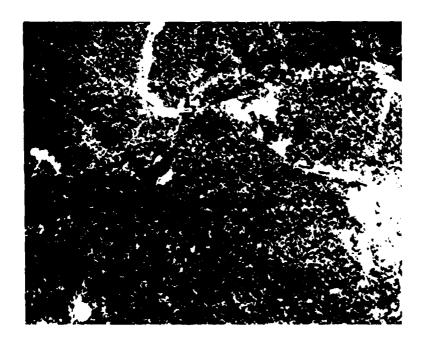


Fig. 4t File 20

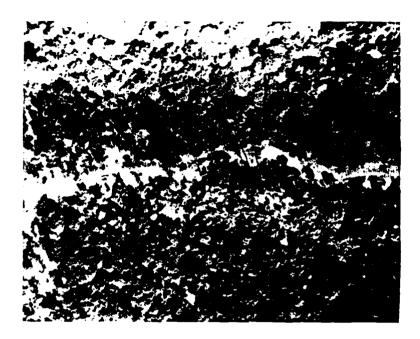


Fig. 4u File 21

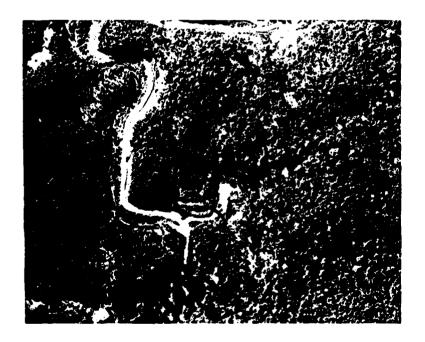


Fig. 4v File 22

IMAGE FILE 1

(5,4)	POSSIBLE TARGET P DETERMINED BY THE	
(3,4)		
(6, 4)		IMAGE FILE 1
(3,3)	(5,4)	POSSIBLE TARGET POSITIONS DETERMINED BY BOTH FEATURES
(4,4)	(6, 4)	
(2, 5)	(-3; 4)	
(2, 3)	(2, 4)	(5, 4)
(7, 4)	(4,4)	(3,4)
(2, 4)	(6, 6)	(6, 4)
(6,3)	(2, 5)	(4, 4)
	(2, 3)	(2, 5)
	(2, 6)	(2, 3)
	(3, 5)	(2, 4)

IMAGE FILE 2

POSSIBLE TARGET POSITIONS DETERMINED BY THE TEXTURE FEATURE

1MAGE FILE 2

(15, 14)

(14, 15)	POSSIBLE TARGET DETERMINED BY TH	POSITIONS NE GRADIENT FEATURE
(2, 6)		IMAGE FILE 2
(3, 6)	(14, 15)	POSSIBLE TARGET POSITIONS
(4, 10)	(3,5)	DETERMINED BY BOTH FEATURES
(2, 8)	(3, 6)	
(3,5)	(13, 15)	(14, 15)
(15, 14)	(14, 7)	(3,6)
(5,4)	(2, 12)	(3, 5)
(14, 7)	(4, 2)	(15, 14)
(14, 10)	(15, 10)	(14, 7)
	(7. 4)	

IMAGE FILE 3

	POSSIBLE TARGET P	
(15, 13)	DETERMINED BY THE	GRADIENT FEATURE
(2, 6)		
(11, 7)	(2, 6)	1MAGE FILE 3
(14, 8)	(B, E)	POSSIBLE TARGET POSITIONS
(2, 5)	(2, 3)	DETERMINED BY BOTH FEATURES
(13, 10)	(6, 9)	
(2, 8)	(14, 9)	(2 , 6)
(€, 7)	(13, 8)	(2, 5)
(10, 6)	(2, 5)	(2, ε)
(12, 9)	(15, 8)	
	(3,8)	
	(10, 5)	

IMAGE FILE 4

POSSIBLE TARGET POSITIONS
DETERMINED BY THE TEXTURE FEATURE

IMAGE FILE 4

	POSSIBLE TARGET P	
(8,15)	DETERMINED BY THE	CRADIENT FEATURE
(9, 15)		IMAGE FILE 4
(3, 6)	(8,15)	POSSIBLE TARGET POSITIONS
(8,14)	(15, 14)	DETERMINED BY BOTH FEATURES
(11, 12)	(10, 10)	
(6, 13)	(11, 11)	(8, 15)
(12, 3)	(10, 12)	(9, 15)
(15/14)	(11, 12)	(3,6)
(2, 6)	(8, 14)	(8,14)
(%, 14)	(12, 12)	(11, 12)
	(3,6)	(15, 14)
	(9, 15)	

IMAGE FILE 5

POSSIBLE	TARGET	POSITIONS	
DETERMINE	D BY 7	HE GRADIENT	FEATURE

(10, 9)	DETERMINED BY TH	E GRADIENT FEATURE
(9, 9)		
(3, 10)	(5, 2)	IMAGE FILE 5
(4, 3)	(7, 2)	POSSIBLE TARGET POSITIONS DETERMINED BY BOTH FEATURES
(3,3)	(-2, 15)	
(12) 7)	(9/ 9)	
(5, 7)	(6, 2)	(10, 9)
(15, 3)	(3, 3)	(9,9)
(15) 9)	(13, 2)	(-3, -3)
(2, 4)	(15, 9)	(15. 9)
•	(10, 9)	
	(8, 2)	

IMAGE FILE 7

POSSIBLE TARGET POSITIONS DETERMINED BY THE TEXTURE FEATURE

IMAGE FILE 7

POSSIBLE TARGET POSITIONS DETERMINED BY THE GRADIENT FEATURE

(14)	3)	DETERMINED BY THE	GRADIENT FEATURE
(3,	6)		IMAGE FILE 7
(5,	7)	(13, 7)	POSSIBLE TARGET POSITIONS
(13)	7)	(2, 8)	DETERMINED BY BOTH FEATURES
(15)	7)	(9,8)	
(14,	7)	(2, 7)	(14, 8)
(12,	&) .	(14, 9)	(13. 7)
(12)	9)	(14, 8)	(15, 7)
(4,	6)	(13, 8)	
15,	8)	(12, 7)	
		(12, 8)	
		(15, 7)	

IMAGE FILE 8

POSSIBLE T	ARGET	POSITI	ONS	
DETERMINED	BY TI	HE GRAD	IENT	FEATURE

(9,10)	DETERMINED BY (HE GRADIENT FEATURE
(8,10)		
(8,1,1)	/ 1 / 1 / 1 / 1 / 1 / 1 / 1 / 1 / 1 / 1	IMAGE FILE 8
(3,11)	(14, 9)	POSSIBLE TARGET POSITIONS
	(14, 10)	DETERMINED BY BOTH FEATURES
(5,7)	(14, 11)	
(4, 8)	(13, 9)	(4,8)
(15, 10)	(4,8)	
(12, 9)	(11, 11)	(12, 9)
(14, 9)	(12, 9)	(14, 9)
(7, 12)		
\	(2, 8)	
	(3,7)	
	(13,11)	·

IMAGE FILE 9

PUSSIBLE TARGET POSITIONS
DETERMINED BY THE TEXTURE FEATURE

IMAGE FILE 9

	POSSIBLE TARGET	
(-9, -4)	DETERMINED BY TH	HE GRADIENT FEATURE
(12, 14)		
(6, 5)		TMAGE FILE 9
	(2, 4)	FORCETTALE TARGET ROOTTALE
(7,10)	(7-11)	POSSIBLE TARGET POSITIONS DETERMINED BY BOTH FEATURES
(7, 5)	(13, 12)	
(5, 11)	(14, 18)	
(7,11)	/40 E)	(9,4)
(13, 12)	(13, 5)	(7, 11)
Carlotte a and	(15, 12)	
(10) (5)		(1%, 12)
(6, 7)	(9, 14)	
04 7	(10, €)	
	(14,12)	
	(11, 3)	

TMAGE FILE 10

(4, ♥)	POSSIBLE TARG DETERMINED BY			
(13, 10)				
(a, ç)		TMAGE	FILE *0	
(Z, 7)	(3, 15)	POSSIBLE TARGET POSITIONS		
(7 - 3)	(4,15)	DETERMINED BY BOTH REATURES		
	(4, 7)			
(S _i (S)	(5,15)		(4, 7)	
(2, 7)	(3, 6)		C 5, 15)	
(5, 7)	(10, 9)		(5, 7)	
(14, 14)	(5, 7)			
(13/8)	(4, 8)			
•	(13, 4)			
IMAGE FILE 15	/ E. E)	IMAGE FILE	. 	
POSSIBLE TARGET POSITIONS DETERMINED BY THE TEXTURE FEATURE		POSSIBLE TARGET POSITIONS DETERMINED BY THE GRADIENT FLATURE		
(12. 5)		(12. 5)		
(7, 4)		(15, ₺)		
(9, 4)	•	(5, C)	TMOSE STUDIES	
(3, 4)	•	(4,8)	TMAGE FILE 15	
(হ. ই)	(3 2)	POSSIBLE TARGET POSITIONS DETERMINED BY BOTH FEATURES	
(13,13	•	(12, 15)		
(to 4)	(14, 15)		
(3.11	y	(7, 2)	(12, 5)	
€ 2. 5	:	(T. A)	(7, 4)	
(10) 5	3	(3,7)	(13 5)	
(15) 7	· y	(13, 5)	(7,13)	
(3, 5	;	(3, 9)		
(5. 2	?)	(8,3)		
(7.15	7.)	(13, 15)		
		1		

IMAGE FILE	11 IMAGE FILE	12 IMAGE FILE 13	IMAGE FILE 14
(6, 4)	(15/-5)	(9,9)	(-2/-4)
(135-77)	(10, 12)	(-6,.0)	(4,4)
(13, 8)	(13, 3)	(77-6)	(3,4)
(13, 3)	(13, 2)	(-2, 15)	(S) 5 5
(13, 10)	(11/14)	(5, 4)	(4, 15)
(14, 12)	(14, 5)	(= #; - &;)	(2, 3)
(11, 13)	(10,18)	(6, 9)	(4. <i>E</i>)
(4, 6°	(12, 9)	(5,8)	(2,11)
(13, 6)	(9,13)	(15, 5)	(15, 8)
(8,15)	(9,9)	((14, 7)

IMAGE FILE 17

IMAGE FILE 18

IMAGE FILE 19

			IMAGE FILE 20)
				IMAGE FILE 11
(3, 2)	,,,			
(-2, 4)	(15, 2) (-9, 3)	(15, 4)		
(2, 15)	(1.5, 1.3)	(12,15)	(8,5)	
(13, 5)	(12, 12)	(14, 3)	(13. 5)	(S, 2)
(2, 2)	(3,3)	(9, 2)	(11.18)	(18, 111)
(3, 15)	(4.12)	(-5, 4)	(11,14)	(6, 3)
(15, 5)	(14,13)	(2, 3)	(-6, -7)	(8, 4) (7, 2)
(2, 8)	(15, 14)	(14, 4)	(15, 6)	(13, 9)
(10, 6)	(3, 14)	(-6, 4)	(10, 13) (14, -7)	(7, 3)
(190 - 07	(3) 9)	(4, 15)	(15) (7)	C 25 (7)
		(-6, 15)	(15, 8)	(8, 2)
				(7.5)

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19. < EY WORDS (Continue on reverse side if necessary and identify by black number) Fisher's linear discriminant Statistical image segmentation Infrared images; Reconnaissance images Texture feature; Gradient feature			
Experiments on statistical image segmentation are performed on infrared image data base and reconnaissance image data sets by using respectively Fisher's linear discriminant and statistical features including texture and average gradient. The Fisher's linear discriminant is shown experimentally to be very effective in the segmentation of infrared images.			